WELSH JOINT EDUCATION COMMITTEE CYD-BWYLLGOR ADDYSG CYMRU

General Certificate of Education

Tystysgrif Addysg Gyffredinol

Advanced Level/Advanced Subsidiary

Safon Uwch/Uwch Gyfrannol

MATHEMATICS C4

Pure Mathematics

Specimen Paper 2005/2006

 $(1\frac{1}{2} \text{ hours})$

INSTRUCTIONS TO CANDIDATES

Answer all questions.

INFORMATION FOR CANDIDATES

A calculator may be used for this paper.

A formula booklet is available and may be used.

The number of marks is given in brackets at the end of each question or part-question.

You are reminded of the necessity for good English and orderly presentation in your answers.

the term in x^3 . Write down and simplify the binomial expansion of $(1+2x)^{-\frac{1}{2}}$ up to and including

term in x^3 . State the range of values of x for which the expansion is valid. Find the expansion of $(1+2x)^{\frac{1}{2}}$ $(1-x)^2$ in ascending powers of x up to and including the [7]

- 12 (a) Use a counter-example to show the statement $\cos 2\theta = 2\cos\theta$ is not always
- (b) Showing all your working, find the values of θ between 0° and 360° satisfying

$$3\cos 2\theta = 1 - \sin \theta.$$
 [6]

çu equation Showing all your working, find the values of θ between 0° and 360° satisfying the

$$5\sin\theta + 4\cos\theta = 3. \tag{7}$$

4 (a) Express $\frac{3x^2+2x+1}{3}$ $x^{2}(x-1)$ in terms of partial fractions.

[4]

(b) Find
$$\int \frac{3x^2 + 2x + 1}{x^2(x-1)} dx$$
. [3]

Ċ normal to C at the point P, whose parameter is p, is A curve C has parametric equations $x = at^2$, y = 2at. Show that the equation of the

$$px + y - 2ap - ap^3 = 0.$$

The normal to C at P meets the x-axis at Q. meets the x-axis at R. Find the length of QR. The perpendicular from P to the x-axis

9 Actinium is a radioactive substance which decays slowly

mass is proportional to the value of x. Initially, 2 kg of actinium is present and the rate of decay of its mass is 64 g/year. Subsequently, t years later when the actinium has a mass x kg, the rate of decrease of

Show that $\frac{dx}{dt} = -0.032x$. [3]

(a)

6 Deduce that $t = \frac{125}{4} \ln \left(\frac{2}{x} \right)$.

5

- 0 Find the value of t when half the actinium has decayed, giving your answer correct to two decimal places.
- .7 between x = 1 and x = e is rotated about the x-axis. Find the volume of the solid generated when the portion of the curve $y = \sqrt{x^3} \ln x$ [6]
- 00 (a) Show that

$$\int_0^{\frac{\pi}{4}} \cos^2 \theta \, d\theta = \frac{\pi}{8} + \frac{1}{4}.$$
 [4]

(b) Use the substitution $x = 3\tan\theta$ to evaluate

$$\int_0^3 \frac{27}{(9+x^2)^2} dx.$$
 [6]

9. The vector equations of two lines are

$$r = 2i + j + \lambda(i + j + 2k),$$

 $r = 2i + 2j + tk + \mu(i + 2j + k),$

where t is a constant.

- (a) of the point of intersection. Given that the two lines intersect, show that t = -1 and find the position vector [6]
- (b) Find the acute angle between the lines, giving your answer correct to the nearest degree. [6]