

973/01

**MATHEMATICS C1**

**Pure Mathematics**

P.M. MONDAY, 10 January 2005

(1½ hours)

# NEW SPECIFICATION

## ADDITIONAL MATERIALS

In addition to this examination paper, you will need:

- a 12 page answer book;
- a Formula Booklet.

## INSTRUCTIONS TO CANDIDATES

Answer **all** questions.

Calculators are **not** allowed for this paper.

## INFORMATION FOR CANDIDATES

The number of marks is given in brackets at the end of each question or part-question.

You are reminded of the necessity for good English and orderly presentation in your answers.

1. The points  $A$  and  $B$  have coordinates  $(2, 3)$  and  $(5, 9)$  respectively. The line through  $B$  perpendicular to  $AB$  meets the  $x$ -axis at the point  $C$ .

(a) Show that the equation of the line  $BC$  is

$$x + 2y - 23 = 0. \quad [6]$$

(b) Find the coordinates of  $C$ . [1]

The point  $D$  has coordinates  $(24, 1)$ . The line through  $A$  parallel to the line  $CD$  intersects the line  $BC$  in the point  $E$ .

(c) Show that the coordinates of  $E$  are  $(7, 8)$ . [5]

(d) Find the length of  $CE$ . [2]

2. Simplify

$$\frac{6 + \sqrt{7}}{\sqrt{7} - 2},$$

expressing your answer in surd form. [4]

3. A curve  $C$  has equation

$$y = 2x^3 - 6x^2 + 12.$$

(a) Find the coordinates of the stationary points of  $C$  and determine the nature of each of those points. [7]

(b) Sketch  $C$ . [3]

(c) State, giving a reason, the number of real roots of the equation

$$2x^3 - 6x^2 + 12 = 0. \quad [2]$$

4. (a) Find all the factors of the polynomial

$$3x^3 + 2x^2 - 19x + 6. \quad [6]$$

(b) Find the remainder when  $3x^3 + 2x^2 - 19x + 6$  is divided by  $x + 1$ . [3]

5. Express the quadratic expression  $x^2 - 14x + 55$  in the form  $(x - a)^2 + b$ , where the values of the constants  $a$  and  $b$  are to be determined. Hence show that  $x^2 - 14x + 55$  is positive for all values of  $x$ . [5]

6. The curve  $C$  has equation

$$y = 4x^2 - 7x + 11,$$

and the line  $L$  has equation

$$y = 5x + k,$$

where  $k$  is a constant. Given that  $L$  intersects  $C$  in two distinct points, show that  $k > 2$ .

[6]

7. Differentiate  $x^2 + 4x + 3$  from first principles.

[5]

8. The curve  $C$  has equation  $y = 3x^{\frac{3}{2}} - \frac{32}{x}$ .

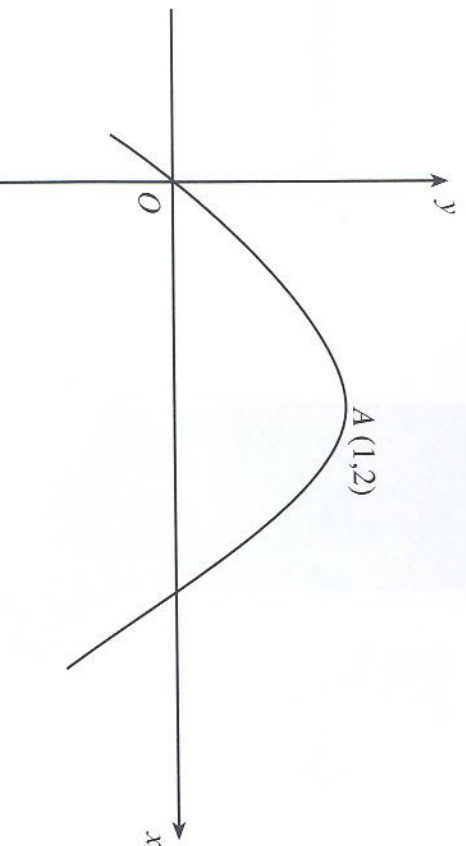
(a) Find the equation of the tangent to  $C$  at the point where  $x = 4$ .

[7]

(b) Find the equation of the normal to  $C$  at the point where  $x = 4$ .

[21]

9.



The diagram shows the graph of  $y = f(x)$ . The curve passes through the origin, and has a maximum point at  $(1, 2)$ .

Sketch on separate diagrams the graphs of

(a)  $y = f(x) + 4,$

(b)  $y = f(x + 3),$

(c)  $y = f(2x),$

giving the coordinates of the maximum point in each case.

[2], [2], [2]

10. (a) Write down the expansion of  $(a + b)^4$ .

[2]

(b) In the binomial expansion of  $(a + 2x)^4$ , the coefficient of the term in  $x^2$  is twelve times the coefficient of the term in  $x^3$ . Find the value of  $a$ .

[3]